1 Calculate the dot products $u \cdot v$ and $u \cdot w$ and $u \cdot (v + w)$ and $w \cdot v$:

$$u = \begin{bmatrix} -.6 \\ .8 \end{bmatrix}$$
 $v = \begin{bmatrix} 3 \\ 4 \end{bmatrix}$ $w = \begin{bmatrix} 8 \\ 6 \end{bmatrix}$.

- Compute the lengths ||u|| and ||v|| and ||w|| of those vectors. Check the Schwarz inequalities $|u \cdot v| \le ||u|| ||v||$ and $||v \cdot w|| \le ||v|| ||w||$.
- Find unit vectors in the directions of v and w in Problem 1, and the cosine of the angle θ . Choose vectors a, b, c that make 0° , 90° , and 180° angles with w.
- 4 For any unit vectors v and w, find the dot products (actual numbers) of
 - (a) v and -v (b) v + w and v w (c) v 2w and v + 2w
- Find unit vectors u_1 and u_2 in the directions of v = (3, 1) and w = (2, 1, 2). Find unit vectors U_1 and U_2 that are perpendicular to u_1 and u_2 .
- 7 Find the angle θ (from its cosine) between these pairs of vectors:

(a)
$$v = \begin{bmatrix} 1 \\ \sqrt{3} \end{bmatrix}$$
 and $w = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$ (b) $v = \begin{bmatrix} 2 \\ 2 \\ -1 \end{bmatrix}$ and $w = \begin{bmatrix} 2 \\ -1 \\ 2 \end{bmatrix}$ (c) $v = \begin{bmatrix} 1 \\ \sqrt{3} \end{bmatrix}$ and $w = \begin{bmatrix} -1 \\ \sqrt{3} \end{bmatrix}$ (d) $v = \begin{bmatrix} 3 \\ 1 \end{bmatrix}$ and $w = \begin{bmatrix} -1 \\ -2 \end{bmatrix}$.

- 8 True or false (give a reason if true or a counterexample if false):
 - (a) If u is perpendicular (in three dimensions) to v and w, those vectors v and w are parallel.
 - (b) If u is perpendicular to v and w, then u is perpendicular to v + 2w.
 - (c) If u and v are perpendicular unit vectors then $||u v|| = \sqrt{2}$.
- With v = (1, 1) and w = (1, 5) choose a number c so that w cv is perpendicular to v. Then find the formula that gives this number c for any nonzero v and w. (Note: cv is the "projection" of w onto v.)