


## PROBLEMS

1, 2, 3 = straightforward, intermediate, challenging □ = full solution available in the *Student Solutions Manual and Study Guide*

WEB = solution posted at <http://www.saunderscollege.com/physics/>  = Computer useful in solving problem  = Interactive Physics

 = paired numerical/symbolic problems

## Section 2.1 Displacement, Velocity, and Speed

1. The position of a pinewood derby car was observed at various times; the results are summarized in the table below. Find the average velocity of the car for (a) the first second, (b) the last 3 s, and (c) the entire period of observation.

$x$ (m)	0	2.3	9.2	20.7	36.8	57.5
$t$ (s)	0	1.0	2.0	3.0	4.0	5.0

2. A motorist drives north for 35.0 min at 85.0 km/h and then stops for 15.0 min. He then continues north, traveling 130 km in 2.00 h. (a) What is his total displacement? (b) What is his average velocity?
3. The displacement versus time for a certain particle moving along the  $x$  axis is shown in Figure P2.3. Find the average velocity in the time intervals (a) 0 to 2 s, (b) 0 to 4 s, (c) 2 s to 4 s, (d) 4 s to 7 s, (e) 0 to 8 s.

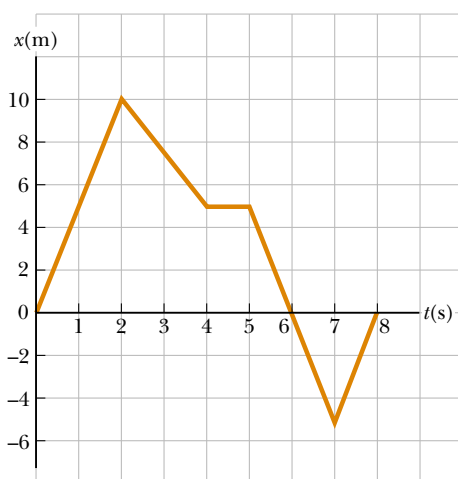


Figure P2.3 Problems 3 and 11.

4. A particle moves according to the equation  $x = 10t^2$ , where  $x$  is in meters and  $t$  is in seconds. (a) Find the average velocity for the time interval from 2.0 s to 3.0 s. (b) Find the average velocity for the time interval from 2.0 s to 2.1 s.
5. A person walks first at a constant speed of 5.00 m/s along a straight line from point  $A$  to point  $B$  and then back along the line from  $B$  to  $A$  at a constant speed of 3.00 m/s. What are (a) her average speed over the entire trip and (b) her average velocity over the entire trip?

6. A person first walks at a constant speed  $v_1$  along a straight line from  $A$  to  $B$  and then back along the line from  $B$  to  $A$  at a constant speed  $v_2$ . What are (a) her average speed over the entire trip and (b) her average velocity over the entire trip?

## Section 2.2 Instantaneous Velocity and Speed

7. At  $t = 1.00$  s, a particle moving with constant velocity is located at  $x = -3.00$  m, and at  $t = 6.00$  s the particle is located at  $x = 5.00$  m. (a) From this information, plot the position as a function of time. (b) Determine the velocity of the particle from the slope of this graph.
8. The position of a particle moving along the  $x$  axis varies in time according to the expression  $x = 3t^2$ , where  $x$  is in meters and  $t$  is in seconds. Evaluate its position (a) at  $t = 3.00$  s and (b) at  $3.00$  s +  $\Delta t$ . (c) Evaluate the limit of  $\Delta x/\Delta t$  as  $\Delta t$  approaches zero to find the velocity at  $t = 3.00$  s.

- WEB 9. A position–time graph for a particle moving along the  $x$  axis is shown in Figure P2.9. (a) Find the average velocity in the time interval  $t = 1.5$  s to  $t = 4.0$  s. (b) Determine the instantaneous velocity at  $t = 2.0$  s by measuring the slope of the tangent line shown in the graph. (c) At what value of  $t$  is the velocity zero?

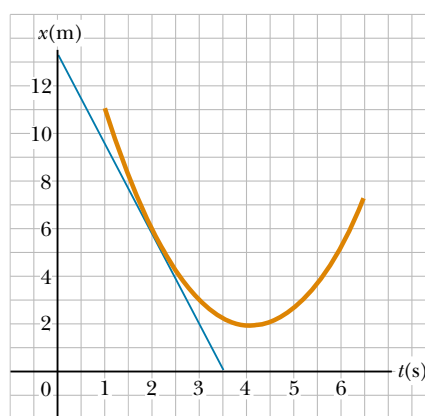


Figure P2.9

10. (a) Use the data in Problem 1 to construct a smooth graph of position versus time. (b) By constructing tangents to the  $x(t)$  curve, find the instantaneous velocity of the car at several instants. (c) Plot the instantaneous velocity versus time and, from this, determine the average acceleration of the car. (d) What was the initial velocity of the car?

11. Find the instantaneous velocity of the particle described in Figure P2.3 at the following times: (a)  $t = 1.0$  s, (b)  $t = 3.0$  s, (c)  $t = 4.5$  s, and (d)  $t = 7.5$  s.

### Section 2.3 Acceleration

12. A particle is moving with a velocity of  $60.0$  m/s in the positive  $x$  direction at  $t = 0$ . Between  $t = 0$  and  $t = 15.0$  s, the velocity decreases uniformly to zero. What was the acceleration during this  $15.0$ -s interval? What is the significance of the sign of your answer?
13. A  $50.0$ -g superball traveling at  $25.0$  m/s bounces off a brick wall and rebounds at  $22.0$  m/s. A high-speed camera records this event. If the ball is in contact with the wall for  $3.50$  ms, what is the magnitude of the average acceleration of the ball during this time interval? (Note:  $1$  ms =  $10^{-3}$  s.)
14. A particle starts from rest and accelerates as shown in Figure P2.14. Determine: (a) the particle's speed at  $t = 10$  s and at  $t = 20$  s, and (b) the distance traveled in the first  $20$  s.

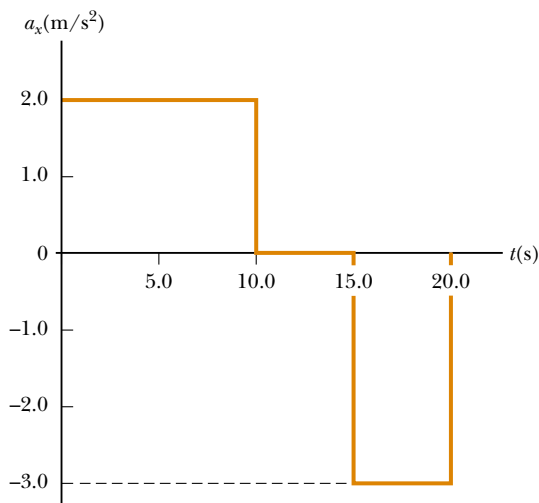


Figure P2.14

15. A velocity–time graph for an object moving along the  $x$  axis is shown in Figure P2.15. (a) Plot a graph of the acceleration versus time. (b) Determine the average acceleration of the object in the time intervals  $t = 5.00$  s to  $t = 15.0$  s and  $t = 0$  to  $t = 20.0$  s.
16. A student drives a moped along a straight road as described by the velocity–time graph in Figure P2.16. Sketch this graph in the middle of a sheet of graph paper. (a) Directly above your graph, sketch a graph of the position versus time, aligning the time coordinates of the two graphs. (b) Sketch a graph of the acceleration versus time directly below the  $v_x$ - $t$  graph, again aligning the time coordinates. On each graph, show the

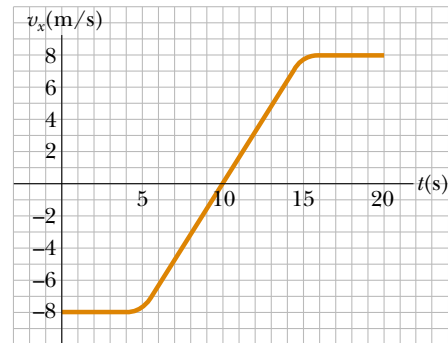


Figure P2.15

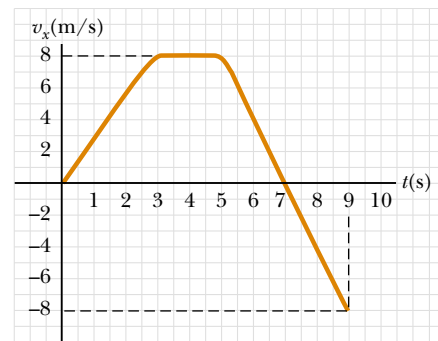


Figure P2.16

numerical values of  $x$  and  $a_x$  for all points of inflection. (c) What is the acceleration at  $t = 6$  s? (d) Find the position (relative to the starting point) at  $t = 6$  s. (e) What is the moped's final position at  $t = 9$  s?

- WEB 17. A particle moves along the  $x$  axis according to the equation  $x = 2.00 + 3.00t - t^2$ , where  $x$  is in meters and  $t$  is in seconds. At  $t = 3.00$  s, find (a) the position of the particle, (b) its velocity, and (c) its acceleration.
18. An object moves along the  $x$  axis according to the equation  $x = (3.00t^2 - 2.00t + 3.00)$  m. Determine (a) the average speed between  $t = 2.00$  s and  $t = 3.00$  s, (b) the instantaneous speed at  $t = 2.00$  s and at  $t = 3.00$  s, (c) the average acceleration between  $t = 2.00$  s and  $t = 3.00$  s, and (d) the instantaneous acceleration at  $t = 2.00$  s and  $t = 3.00$  s.
19. Figure P2.19 shows a graph of  $v_x$  versus  $t$  for the motion of a motorcyclist as he starts from rest and moves along the road in a straight line. (a) Find the average acceleration for the time interval  $t = 0$  to  $t = 6.00$  s. (b) Estimate the time at which the acceleration has its greatest positive value and the value of the acceleration at that instant. (c) When is the acceleration zero? (d) Estimate the maximum negative value of the acceleration and the time at which it occurs.

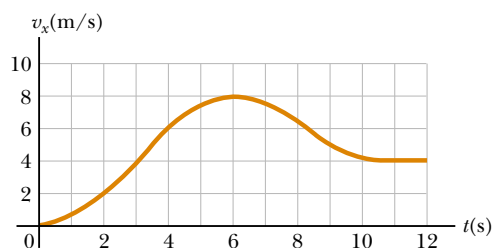


Figure P2.19

### Section 2.4 Motion Diagrams

20. Draw motion diagrams for (a) an object moving to the right at constant speed, (b) an object moving to the right and speeding up at a constant rate, (c) an object moving to the right and slowing down at a constant rate, (d) an object moving to the left and speeding up at a constant rate, and (e) an object moving to the left and slowing down at a constant rate. (f) How would your drawings change if the changes in speed were not uniform; that is, if the speed were not changing at a constant rate?

### Section 2.5 One-Dimensional Motion with Constant Acceleration

21. Jules Verne in 1865 proposed sending people to the Moon by firing a space capsule from a 220-m-long cannon with a final velocity of 10.97 km/s. What would have been the unrealistically large acceleration experienced by the space travelers during launch? Compare your answer with the free-fall acceleration,  $9.80 \text{ m/s}^2$ .
22. A certain automobile manufacturer claims that its super-deluxe sports car will accelerate from rest to a speed of  $42.0 \text{ m/s}$  in  $8.00 \text{ s}$ . Under the (improbable) assumption that the acceleration is constant, (a) determine the acceleration of the car. (b) Find the distance the car travels in the first  $8.00 \text{ s}$ . (c) What is the speed of the car  $10.0 \text{ s}$  after it begins its motion, assuming it continues to move with the same acceleration?
23. A truck covers  $40.0 \text{ m}$  in  $8.50 \text{ s}$  while smoothly slowing down to a final speed of  $2.80 \text{ m/s}$ . (a) Find its original speed. (b) Find its acceleration.
24. The minimum distance required to stop a car moving at  $35.0 \text{ mi/h}$  is  $40.0 \text{ ft}$ . What is the minimum stopping distance for the same car moving at  $70.0 \text{ mi/h}$ , assuming the same rate of acceleration?
- WEB 25. A body moving with uniform acceleration has a velocity of  $12.0 \text{ cm/s}$  in the positive  $x$  direction when its  $x$  coordinate is  $3.00 \text{ cm}$ . If its  $x$  coordinate  $2.00 \text{ s}$  later is  $-5.00 \text{ cm}$ , what is the magnitude of its acceleration?
26. Figure P2.26 represents part of the performance data of a car owned by a proud physics student. (a) Calculate from the graph the total distance traveled. (b) What distance does the car travel between the times  $t = 10 \text{ s}$  and  $t = 40 \text{ s}$ ? (c) Draw a graph of its ac-

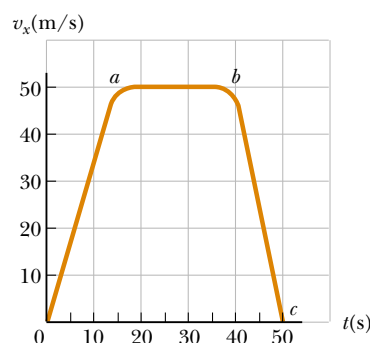


Figure P2.26

celeration versus time between  $t = 0$  and  $t = 50 \text{ s}$ .

- (d) Write an equation for  $x$  as a function of time for each phase of the motion, represented by (i)  $0a$ , (ii)  $ab$ , (iii)  $bc$ . (e) What is the average velocity of the car between  $t = 0$  and  $t = 50 \text{ s}$ ?
27. A particle moves along the  $x$  axis. Its position is given by the equation  $x = 2.00 + 3.00t - 4.00t^2$  with  $x$  in meters and  $t$  in seconds. Determine (a) its position at the instant it changes direction and (b) its velocity when it returns to the position it had at  $t = 0$ .
28. The initial velocity of a body is  $5.20 \text{ m/s}$ . What is its velocity after  $2.50 \text{ s}$  (a) if it accelerates uniformly at  $3.00 \text{ m/s}^2$  and (b) if it accelerates uniformly at  $-3.00 \text{ m/s}^2$ ?
29. A drag racer starts her car from rest and accelerates at  $10.0 \text{ m/s}^2$  for the entire distance of  $400 \text{ m}$  ( $\frac{1}{4} \text{ mi}$ ). (a) How long did it take the race car to travel this distance? (b) What is the speed of the race car at the end of the run?
30. A car is approaching a hill at  $30.0 \text{ m/s}$  when its engine suddenly fails, just at the bottom of the hill. The car moves with a constant acceleration of  $-2.00 \text{ m/s}^2$  while coasting up the hill. (a) Write equations for the position along the slope and for the velocity as functions of time, taking  $x = 0$  at the bottom of the hill, where  $v_i = 30.0 \text{ m/s}$ . (b) Determine the maximum distance the car travels up the hill.
31. A jet plane lands with a speed of  $100 \text{ m/s}$  and can accelerate at a maximum rate of  $-5.00 \text{ m/s}^2$  as it comes to rest. (a) From the instant the plane touches the runway, what is the minimum time it needs before it can come to rest? (b) Can this plane land at a small tropical island airport where the runway is  $0.800 \text{ km}$  long?
32. The driver of a car slams on the brakes when he sees a tree blocking the road. The car slows uniformly with an acceleration of  $-5.60 \text{ m/s}^2$  for  $4.20 \text{ s}$ , making straight skid marks  $62.4 \text{ m}$  long ending at the tree. With what speed does the car then strike the tree?
33. *Help! One of our equations is missing!* We describe constant-acceleration motion with the variables and parameters  $v_{xi}$ ,  $v_{xf}$ ,  $a_x$ ,  $t$ , and  $x_f - x_i$ . Of the equations in Table 2.2, the first does not involve  $x_f - x_i$ . The second does not contain  $a_x$ , the third omits  $v_{xf}$ , and the last



**Figure P2.37** (Left) Col. John Stapp on rocket sled. (Courtesy of the U.S. Air Force)  
(Right) Col. Stapp's face is contorted by the stress of rapid negative acceleration. (Photri, Inc.)

leaves out  $t$ . So to complete the set there should be an equation *not* involving  $v_{xi}$ . Derive it from the others. Use it to solve Problem 32 in one step.

34. An indestructible bullet 2.00 cm long is fired straight through a board that is 10.0 cm thick. The bullet strikes the board with a speed of 420 m/s and emerges with a speed of 280 m/s. (a) What is the average acceleration of the bullet as it passes through the board? (b) What is the total time that the bullet is in contact with the board? (c) What thickness of board (calculated to 0.1 cm) would it take to stop the bullet, assuming the bullet's acceleration through all parts of the board is the same?
35. A truck on a straight road starts from rest, accelerating at  $2.00 \text{ m/s}^2$  until it reaches a speed of 20.0 m/s. Then the truck travels for 20.0 s at constant speed until the brakes are applied, stopping the truck in a uniform manner in an additional 5.00 s. (a) How long is the truck in motion? (b) What is the average velocity of the truck for the motion described?
36. A train is traveling down a straight track at 20.0 m/s when the engineer applies the brakes. This results in an acceleration of  $-1.00 \text{ m/s}^2$  as long as the train is in motion. How far does the train move during a 40.0-s time interval starting at the instant the brakes are applied?
37. For many years the world's land speed record was held by Colonel John P. Stapp, USAF (Fig. P2.37). On March 19, 1954, he rode a rocket-propelled sled that moved down the track at 632 mi/h. He and the sled were safely brought to rest in 1.40 s. Determine (a) the negative acceleration he experienced and (b) the distance he traveled during this negative acceleration.
38. An electron in a cathode-ray tube (CRT) accelerates uniformly from  $2.00 \times 10^4 \text{ m/s}$  to  $6.00 \times 10^6 \text{ m/s}$  over 1.50 cm. (a) How long does the electron take to travel this 1.50 cm? (b) What is its acceleration?
39. A ball starts from rest and accelerates at  $0.500 \text{ m/s}^2$  while moving down an inclined plane 9.00 m long. When it reaches the bottom, the ball rolls up another plane, where, after moving 15.0 m, it comes to rest.

(a) What is the speed of the ball at the bottom of the first plane? (b) How long does it take to roll down the first plane? (c) What is the acceleration along the second plane? (d) What is the ball's speed 8.00 m along the second plane?

40. Speedy Sue, driving at 30.0 m/s, enters a one-lane tunnel. She then observes a slow-moving van 155 m ahead traveling at 5.00 m/s. Sue applies her brakes but can accelerate only at  $-2.00 \text{ m/s}^2$  because the road is wet. Will there be a collision? If so, determine how far into the tunnel and at what time the collision occurs. If not, determine the distance of closest approach between Sue's car and the van.

## Section 2.6 Freely Falling Objects

*Note:* In all problems in this section, ignore the effects of air resistance.

41. A golf ball is released from rest from the top of a very tall building. Calculate (a) the position and (b) the velocity of the ball after 1.00 s, 2.00 s, and 3.00 s.

42. *Every morning at seven o'clock  
There's twenty terriers drilling on the rock.  
The boss comes around and he says, "Keep still  
And bear down heavy on the cast-iron drill  
And drill, ye terriers, drill." And drill, ye terriers, drill.  
It's work all day for sugar in your tea . . .  
And drill, ye terriers, drill.*

*One day a premature blast went off  
And a mile in the air went big Jim Goff. And drill . . .*

*Then when next payday came around  
Jim Goff a dollar short was found.  
When he asked what for, came this reply:  
"You were docked for the time you were up in the sky." And  
drill . . .*

—American folksong

What was Goff's hourly wage? State the assumptions you make in computing it.

- WEB 43.** A student throws a set of keys vertically upward to her sorority sister, who is in a window 4.00 m above. The keys are caught 1.50 s later by the sister's outstretched hand. (a) With what initial velocity were the keys thrown? (b) What was the velocity of the keys just before they were caught?
- 44.** A ball is thrown directly downward with an initial speed of 8.00 m/s from a height of 30.0 m. How many seconds later does the ball strike the ground?
- 45.** Emily challenges her friend David to catch a dollar bill as follows: She holds the bill vertically, as in Figure P2.45, with the center of the bill between David's index finger and thumb. David must catch the bill after Emily releases it without moving his hand downward. If his reaction time is 0.2 s, will he succeed? Explain your reasoning.



**Figure P2.45** (George Semple)

- 46.** A ball is dropped from rest from a height  $h$  above the ground. Another ball is thrown vertically upward from the ground at the instant the first ball is released. Determine the speed of the second ball if the two balls are to meet at a height  $h/2$  above the ground.
- 47.** A baseball is hit so that it travels straight upward after being struck by the bat. A fan observes that it takes 3.00 s for the ball to reach its maximum height. Find (a) its initial velocity and (b) the maximum height it reaches.
- 48.** A woman is reported to have fallen 144 ft from the 17th floor of a building, landing on a metal ventilator box, which she crushed to a depth of 18.0 in. She suffered only minor injuries. Calculate (a) the speed of the woman just before she collided with the ventilator box, (b) her average acceleration while in contact with the box, and (c) the time it took to crush the box.

- WEB 49.** A daring ranch hand sitting on a tree limb wishes to drop vertically onto a horse galloping under the tree. The speed of the horse is 10.0 m/s, and the distance from the limb to the saddle is 3.00 m. (a) What must be the horizontal distance between the saddle and limb when the ranch hand makes his move? (b) How long is he in the air?
- 50.** A ball thrown vertically upward is caught by the thrower after 20.0 s. Find (a) the initial velocity of the ball and (b) the maximum height it reaches.
- 51.** A ball is thrown vertically upward from the ground with an initial speed of 15.0 m/s. (a) How long does it take the ball to reach its maximum altitude? (b) What is its maximum altitude? (c) Determine the velocity and acceleration of the ball at  $t = 2.00$  s.
- 52.** The height of a helicopter above the ground is given by  $h = 3.00t^3$ , where  $h$  is in meters and  $t$  is in seconds. After 2.00 s, the helicopter releases a small mailbag. How long after its release does the mailbag reach the ground?

(Optional)





## 2.7 Kinematic Equations Derived from Calculus

- 53.** Automotive engineers refer to the time rate of change of acceleration as the "jerk." If an object moves in one dimension such that its jerk  $J$  is constant, (a) determine expressions for its acceleration  $a_x$ , velocity  $v_x$ , and position  $x$ , given that its initial acceleration, speed, and position are  $a_{xi}$ ,  $v_{xi}$ , and  $x_i$ , respectively. (b) Show that  $a_x^2 = a_{xi}^2 + 2J(v_x - v_{xi})$ .
- 54.** The speed of a bullet as it travels down the barrel of a rifle toward the opening is given by the expression  $v = (-5.0 \times 10^7)t^2 + (3.0 \times 10^5)t$ , where  $v$  is in meters per second and  $t$  is in seconds. The acceleration of the bullet just as it leaves the barrel is zero. (a) Determine the acceleration and position of the bullet as a function of time when the bullet is in the barrel. (b) Determine the length of time the bullet is accelerated. (c) Find the speed at which the bullet leaves the barrel. (d) What is the length of the barrel?
- 55.** The acceleration of a marble in a certain fluid is proportional to the speed of the marble squared and is given (in SI units) by  $a = -3.00v^2$  for  $v > 0$ . If the marble enters this fluid with a speed of 1.50 m/s, how long will it take before the marble's speed is reduced to half of its initial value?

## ADDITIONAL PROBLEMS

- 56.** A motorist is traveling at 18.0 m/s when he sees a deer in the road 38.0 m ahead. (a) If the maximum negative acceleration of the vehicle is  $-4.50$  m/s<sup>2</sup>, what is the maximum reaction time  $\Delta t$  of the motorist that will allow him to avoid hitting the deer? (b) If his reaction time is actually 0.300 s, how fast will he be traveling when he hits the deer?



57. Another scheme to catch the roadrunner has failed. A safe falls from rest from the top of a 25.0-m-high cliff toward Wile E. Coyote, who is standing at the base. Wile first notices the safe after it has fallen 15.0 m. How long does he have to get out of the way?
58. A dog's hair has been cut and is now getting longer by 1.04 mm each day. With winter coming on, this rate of hair growth is steadily increasing by 0.132 mm/day every week. By how much will the dog's hair grow during five weeks?
-  59. A test rocket is fired vertically upward from a well. A catapult gives it an initial velocity of 80.0 m/s at ground level. Subsequently, its engines fire and it accelerates upward at 4.00 m/s<sup>2</sup> until it reaches an altitude of 1000 m. At that point its engines fail, and the rocket goes into free fall, with an acceleration of  $-9.80 \text{ m/s}^2$ . (a) How long is the rocket in motion above the ground? (b) What is its maximum altitude? (c) What is its velocity just before it collides with the Earth? (*Hint*: Consider the motion while the engine is operating separate from the free-fall motion.)
-  60. A motorist drives along a straight road at a constant speed of 15.0 m/s. Just as she passes a parked motorcycle police officer, the officer starts to accelerate at 2.00 m/s<sup>2</sup> to overtake her. Assuming the officer maintains this acceleration, (a) determine the time it takes the police officer to reach the motorist. Also find (b) the speed and (c) the total displacement of the officer as he overtakes the motorist.
61. In Figure 2.10a, the area under the velocity–time curve between the vertical axis and time  $t$  (vertical dashed line) represents the displacement. As shown, this area consists of a rectangle and a triangle. Compute their areas and compare the sum of the two areas with the expression on the righthand side of Equation 2.11.
62. A commuter train travels between two downtown stations. Because the stations are only 1.00 km apart, the train never reaches its maximum possible cruising speed. The engineer minimizes the time  $t$  between the two stations by accelerating at a rate  $a_1 = 0.100 \text{ m/s}^2$  for a time  $t_1$  and then by braking with acceleration  $a_2 = -0.500 \text{ m/s}^2$  for a time  $t_2$ . Find the minimum time of travel  $t$  and the time  $t_1$ .
- 63.** In a 100-m race, Maggie and Judy cross the finish line in a dead heat, both taking 10.2 s. Accelerating uniformly, Maggie took 2.00 s and Judy 3.00 s to attain maximum speed, which they maintained for the rest of the race. (a) What was the acceleration of each sprinter? (b) What were their respective maximum speeds? (c) Which sprinter was ahead at the 6.00-s mark, and by how much?
64. A hard rubber ball, released at chest height, falls to the pavement and bounces back to nearly the same height. When it is in contact with the pavement, the lower side of the ball is temporarily flattened. Suppose the maximum depth of the dent is on the order of 1 cm. Compute an order-of-magnitude estimate for the maximum acceleration of the ball while it is in contact with the pavement. State your assumptions, the quantities you estimate, and the values you estimate for them.
65. A teenager has a car that speeds up at 3.00 m/s<sup>2</sup> and slows down at  $-4.50 \text{ m/s}^2$ . On a trip to the store, he accelerates from rest to 12.0 m/s, drives at a constant speed for 5.00 s, and then comes to a momentary stop at an intersection. He then accelerates to 18.0 m/s, drives at a constant speed for 20.0 s, slows down for 2.67 s, continues for 4.00 s at this speed, and then comes to a stop. (a) How long does the trip take? (b) How far has he traveled? (c) What is his average speed for the trip? (d) How long would it take to walk to the store and back if he walks at 1.50 m/s?
66. A rock is dropped from rest into a well. (a) If the sound of the splash is heard 2.40 s later, how far below the top of the well is the surface of the water? The speed of sound in air (at the ambient temperature) is 336 m/s. (b) If the travel time for the sound is neglected, what percentage error is introduced when the depth of the well is calculated?
-  67. An inquisitive physics student and mountain climber climbs a 50.0-m cliff that overhangs a calm pool of water. He throws two stones vertically downward, 1.00 s apart, and observes that they cause a single splash. The first stone has an initial speed of 2.00 m/s. (a) How long after release of the first stone do the two stones hit the water? (b) What was the initial velocity of the second stone? (c) What is the velocity of each stone at the instant the two hit the water?
68. A car and train move together along parallel paths at 25.0 m/s, with the car adjacent to the rear of the train. Then, because of a red light, the car undergoes a uniform acceleration of  $-2.50 \text{ m/s}^2$  and comes to rest. It remains at rest for 45.0 s and then accelerates back to a speed of 25.0 m/s at a rate of  $2.50 \text{ m/s}^2$ . How far behind the rear of the train is the car when it reaches the speed of 25.0 m/s, assuming that the speed of the train has remained 25.0 m/s?
- 69.** Kathy Kool buys a sports car that can accelerate at the rate of  $4.90 \text{ m/s}^2$ . She decides to test the car by racing with another speedster, Stan Speedy. Both start from rest, but experienced Stan leaves the starting line 1.00 s before Kathy. If Stan moves with a constant acceleration of  $3.50 \text{ m/s}^2$  and Kathy maintains an acceleration of  $4.90 \text{ m/s}^2$ , find (a) the time it takes Kathy to overtake Stan, (b) the distance she travels before she catches up with him, and (c) the speeds of both cars at the instant she overtakes him.
-  70. To protect his food from hungry bears, a boy scout raises his food pack with a rope that is thrown over a tree limb at height  $h$  above his hands. He walks away from the vertical rope with constant velocity  $v_{\text{boy}}$ , holding the free end of the rope in his hands (Fig. P2.70).

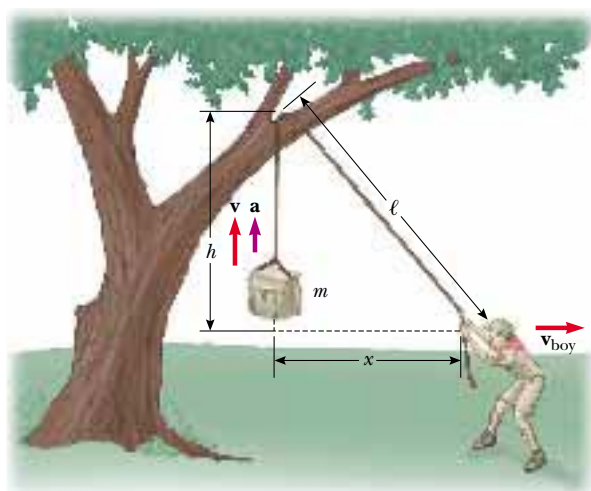


Figure P2.70

(a) Show that the speed  $v$  of the food pack is  $x(x^2 + h^2)^{-1/2} v_{\text{boy}}$ , where  $x$  is the distance he has walked away from the vertical rope. (b) Show that the acceleration  $a$  of the food pack is  $h^2(x^2 + h^2)^{-3/2} v_{\text{boy}}^2$ . (c) What values do the acceleration and velocity have shortly after he leaves the point under the pack ( $x = 0$ )? (d) What values do the pack's velocity and acceleration approach as the distance  $x$  continues to increase?

71. In Problem 70, let the height  $h$  equal 6.00 m and the speed  $v_{\text{boy}}$  equal 2.00 m/s. Assume that the food pack starts from rest. (a) Tabulate and graph the speed–time graph. (b) Tabulate and graph the acceleration–time graph. (Let the range of time be from 0 to 5.00 s and the time intervals be 0.500 s.)

72. Astronauts on a distant planet toss a rock into the air. With the aid of a camera that takes pictures at a steady rate, they record the height of the rock as a function of time as given in Table P2.72. (a) Find the average velocity of the rock in the time interval between each measurement and the next. (b) Using these average veloci-

TABLE P2.72 Height of a Rock versus Time

Time (s)	Height (m)	Time (s)	Height (m)
0.00	5.00	2.75	7.62
0.25	5.75	3.00	7.25
0.50	6.40	3.25	6.77
0.75	6.94	3.50	6.20
1.00	7.38	3.75	5.52
1.25	7.72	4.00	4.73
1.50	7.96	4.25	3.85
1.75	8.10	4.50	2.86
2.00	8.13	4.75	1.77
2.25	8.07	5.00	0.58
2.50	7.90		

ties to approximate instantaneous velocities at the mid-points of the time intervals, make a graph of velocity as a function of time. Does the rock move with constant acceleration? If so, plot a straight line of best fit on the graph and calculate its slope to find the acceleration.

73. Two objects, A and B, are connected by a rigid rod that has a length  $L$ . The objects slide along perpendicular guide rails, as shown in Figure P2.73. If A slides to the left with a constant speed  $v$ , find the speed of B when  $\alpha = 60.0^\circ$ .

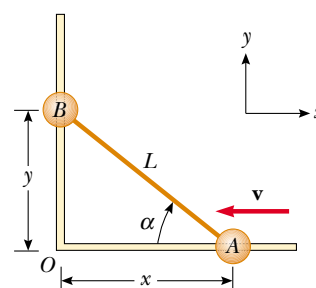


Figure P2.73

## ANSWERS TO QUICK QUIZZES

- 2.1 Your graph should look something like the one in (a). This  $v_x$ - $t$  graph shows that the maximum speed is about 5.0 m/s, which is 18 km/h (= 11 mi/h), and so the driver was not speeding. Can you derive the acceleration–time graph from the velocity–time graph? It should look something like the one in (b).
- 2.2 (a) Yes. This occurs when the car is slowing down, so that the direction of its acceleration is opposite the direction of its motion. (b) Yes. If the motion is in the direction

chosen as negative, a positive acceleration causes a decrease in speed.

- 2.3 The left side represents the final velocity of an object. The first term on the right side is the velocity that the object had initially when we started watching it. The second term is the change in that initial velocity that is caused by the acceleration. If this second term is positive, then the initial velocity has increased ( $v_{xf} > v_{xi}$ ). If this term is negative, then the initial velocity has decreased ( $v_{xf} < v_{xi}$ ).